

Helical magnetic state in the distorted triangular lattice of α -CaCr₂O₄

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Abstract

The magnetic properties of the high temperature α form of the CaCr₂O₄ compound have been investigated for the first time by magnetic susceptibility, specific heat and powder neutron diffraction. The system undergoes a unique magnetic phase transition at 43K to a long range order incommensurate helical phase with magnetic propagation vector $\mathbf{k} = (0, 0.3317(2), 0)$. The magnetic model proposed from neutron diffraction data shows that the plane of rotation of the spins is perpendicular to the wave-vector, and that the magnetic modulation is consistent with two modes belonging to distinct irreducible representations of the group. The magnetic point group 2221' is not compatible with ferroelectricity unlike the CuCrO₂ delafossite [Kimura *et al.*, *Phys. Rev. B*, **78** 140401 (2008)] but predicts the existence of quadratic magnetoelectric effects, discussed based on a Landau analysis.

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I. INTRODUCTION

In recent years, spin-driven ferroelectricity given rise to *giant* magnetoelectric effects has been found in a variety of frustrated magnets, in particular in systems that develop long-wavelength magnetic modulations such as cycloidal or helicoidal states, incommensurate or not with the crystalline lattice. Most of the attention was initially focussed on cycloidal magnets such as TbMnO_3 ¹ for which the inverse Dzyaloshinskii-Moriya² and spin-current model³ predict the onset of a spontaneous polarization when the direction of the modulation (\mathbf{k} -vector) is perpendicular to the spin-rotation axis (\mathbf{e})⁴. More recent work on incommensurate magnetic phases in triangular lattices^{5–10} has established that improper ferroelectric order of similar magnitude also appears in spirals magnets, i.e systems that possess a true magnetic chirality (\mathbf{k} parallel to \mathbf{e}), however requiring another microscopic coupling mechanism such as hybridization effects proposed by Arima¹¹. Those systems are quasi two-dimensional triangular lattices and display a nearly 120° magnetic arrangement in the triangular layers as expected for Heisenberg spins. Improper ferroelectricity predicted by symmetry¹⁰ arguments depends only on the orientation of \mathbf{e} with respect to the crystal axes, often dictated by weak single-ion anisotropy terms.

In this paper, we report for the first time on the magnetic properties of $\alpha\text{-CaCr}_2\text{O}_4$ whose orthorhombic crystal structure¹² is closely related to the structure of delafossites, at the exception of a small distortion of the triangular lattice. The magnetic susceptibility indicates strong antiferromagnetic correlations (Weiss temperature of -893K) and a unique transition to a long-range ordered state at $T_N=43\text{K}$. The specific heat displays a sharp and intense peak around 43K, consistent with a unique transition. Powder neutron diffraction proves the existence of long-range magnetic order below T_N , incommensurate with the crystal lattice with propagation vector $\mathbf{k}=(0,0.3317(2),0)$. The model proposed for the magnetic structure, derived from the neutron data and symmetry considerations, corresponds to a nearly 120° *out of plane* helix, with \mathbf{e} perpendicular to \mathbf{k} . Symmetry analysis using the complete irreducible co-representations of the wave-vector group shows that the point group symmetry of the magnetic state is $2221'$ and can be only stabilized through two successive second-order transitions or through a first-order transition. Whilst in the rhombohedral delafossite such out-of-plane spiral leaves a polar point group, here the spin chirality preserves all proper rotations, predicting the absence of electric polarization

at T_N . However, we show through a Landau analysis of the magnetoelectric free energy that quadratic magnetoelectric effects are allowed by symmetry and should be observed in low magnetic fields.

II. EXPERIMENTAL

The synthesis of polycrystalline α - CaCr_2O_4 followed a two-steps process. A sample of β - CaCr_2O_4 was first prepared in the shape of a rod (6 millimeters in diameter and several centimeters in length), starting from a 1:1 mixture of CaO and Cr_2O_3 heated at 1400°C for 12 hours in an argon flow. This rod was then heated in argon atmosphere by using an image furnace to obtain the high temperature conditions ($T > 1700^\circ\text{C}$) but without reaching the melting temperature. Magnetic susceptibility has been measured using a Superconducting Quantum Interference Device (SQUID, Quantum Design ®) in a magnetic field of 0.3T on warming following a zero-field cooling process. Heat capacity measurements ($C(T)$) were carried out in a Physical Property Measurement System (PPMS, Quantum Design ®) using a semi-adiabatic relaxation method.¹³ Two types of procedures were followed to record zero-field $C(T)$ curves: (i) equally spaced data points registered upon warming and using a small temperature rise of the order of 0.4 K around the transition. The analysis is the standard one in which the so-called 2τ model¹⁴ is used to fit at once both the heating and cooling branches at each point; (ii) a large single-pulse method described in¹⁵ where the temperature is swept across the complete width of the transition, either warming or cooling (temperature rise of 5K). In this case, the heat capacity is derived from a point-by-point analysis of the time response along each of the two branches. In case of a first-order transition, it is known that the former method can yield spurious results,^{16,17} whereas the latter is able to account for both the latent heat and hysteretical features.¹⁵ Neutron diffraction experiments were collected on the WISH diffractometer of the ISIS Facility, Rutherford Appleton Laboratory (UK). Data have been focus on five histograms from detector banks covering 32° each, and are shown for the bank centred at $2\theta = 90^\circ$. A 0.55g sample was placed in a thin wall ($30\mu\text{m}$) vanadium cylindrical can mounted in an helium cryostat. Diffractograms have been recorded in the paramagnetic regime at 70K, at 1.5K and warming in varying temperature steps. Rietveld refinements of the neutron data have been performed with the FullProf

program¹⁸.

III. RESULTS

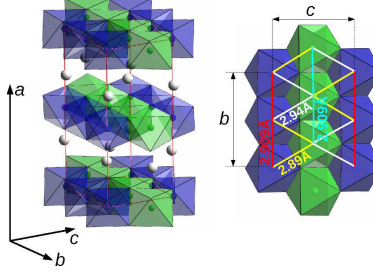


FIG. 1. (Color online) Left) Crystal structure of α - CaCr_2O_4 . CrO_6 octahedra are shown in blue and green colors for the inequivalent Cr_1 and Cr_2 sites (see text for details). The Ca^{2+} ions are shown as light grey spheres. The red thin line marks the crystallographic unit-cell. Right) Projection of the CrO_2 layer onto the bc -plane. Colored thick lines shows the connectivity between first-neighbor Cr ions. The corresponding interatomic distances are shown.

The crystal structure of α - CaCr_2O_4 was first reported by Pausch et al.¹². It crystallizes with orthorhombic symmetry, confirmed by our Electron Microscopy measurements (not shown) in the space group $Pmmn$ (Fig. 1). The structure refined from our neutron diffraction data in the paramagnetic regime at 70K is also consistent with the earlier work¹². There are two inequivalent Cr sites, Cr_1 located at $(0,0,0)$, of $\bar{1}$ symmetry and Cr_2 at position $(0.5047(6), \frac{1}{4}, 0.497(1))$ located on a mirror plane, each site of multiplicity four. The Cr ions are six-coordinated by oxygen in a distorted octahedral configuration. The octahedra share edges to form CrO_2 layers in the bc -plane, leaving a weakly distorted triangular lattice as shown by the different interatomic distances marked in Fig. 1. The CrO_2 layers, separated by Ca^{2+} ions, are stacked along the a -axis of the orthorhombic unit-cell. The in-plane magnetic interactions between Cr can be mediated either by direct exchange through the t_{2g} orbitals or by Cr-O-Cr super-exchange interactions. The interactions between layers can be mediated by super-superexchange interactions through two oxygen atoms, but are expected to be much weaker due to the large interatomic Fe-Fe distance (5.52 \AA at 1.5K).

The inverse magnetic susceptibility (Fig. 2) shows a quasi-linear regime above 250K. A linear fit of the data with a Curie-Weiss law in the temperature range 250K to 350K yields

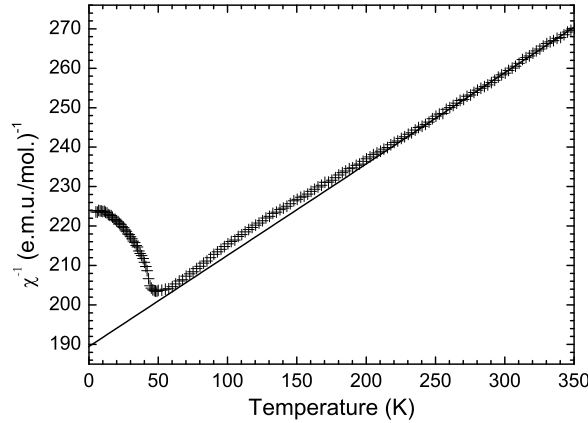


FIG. 2. Inverse molar magnetic susceptibility of α - CaCr_2O_4 as a function of temperature under a magnetic field of 0.3T. The line is a linear fit with a Curie-Weiss law.

a paramagnetic moment of $4.3\mu_B$ per Cr^{3+} ion, and a Weiss temperature of -893K. The value of the paramagnetic moment is larger than the expected value of $3.87\mu_B$ for a pure spin contribution ($S=3/2$) of Cr^{3+} . The reason for this discrepancy is likely related to the limited temperature range of the measurement, much lower than the Weiss temperature, and it seems rather unphysical to ascribe this deviation to a large orbital contribution. The strongly negative Weiss temperature indicates large antiferromagnetic (AFM) interactions. On cooling below 200K, one observe a deviation of the inverse susceptibility from the nearly linear regime followed at $T_N=43\text{K}$ by a more abrupt drop indicative of long-range AFM ordering. There are no evidence of additional transitions from susceptibility measurements at different fields (not shown). The large difference between the value of the Weiss temperature and T_N is inherent to the reduction of dimensionality in this pseudo-2D system as well as magnetic frustration imposed by the triangular geometry.

The left panel of Fig. 3 displays the specific heat, $C(T)$, recorded from the standard and single-pulse methods (see experimental section), while the inset is an enlargement exhibiting the shift between the warming and cooling branches derived from the latter technique. At $T_N=43\text{K}$, a very sharp peak is observed with a full width at half maximum of about 0.5 K. Using a Debye function to fit the high temperature data as an approximation of the lattice specific heat, one can derive the temperature dependence of the magnetic entropy (S_m) shown in right panel of Fig. 3. There is a clear kink at T_N on the $S_m(T)$ curve, but

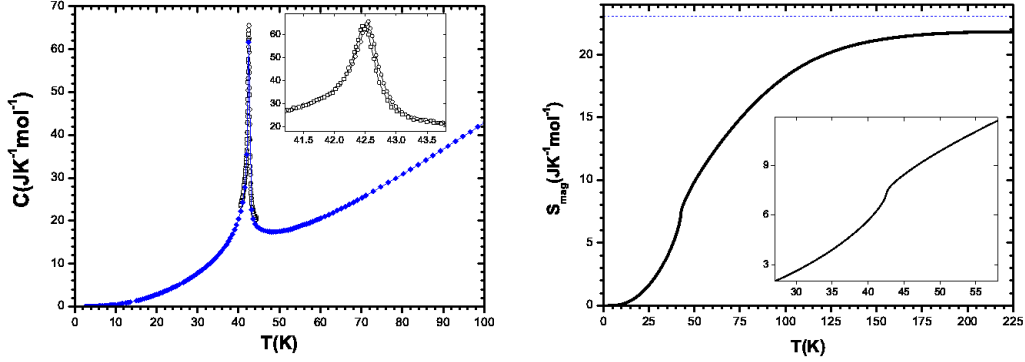


FIG. 3. Left: Specific heat of α - CaCr_2O_4 in zero magnetic field measured by the standard (filled diamonds), single pulse method (open circles) and SPM cooling (open squares) (see text for details of the various techniques). Right: Magnetic entropy obtained by subtracting the lattice contribution estimated by a Debye function to the total specific heat. The inset focus on the temperature region close to T_N . The dashed line indicates the theoretical limit of $2R\ln(4)$.

judging the nature of the transition from this feature only is difficult. The $S_m(T)$ around the transition (Fig. 3 inset) can indeed be regarded either as a broadened jump expected for a first-order transition (FOT) in real materials, i.e. non ideals with the presence of defects- or as a knee typical of a second-order transition (SOT). Two other experimental observations must be considered: first, the nearly perfect superimposition of the $C(T)$ curves derived from the single-pulse and standard method, whilst a substantial part of the latent heat -if present- is supposed to be invisible in the latter technique.¹⁵ Secondly, the temperature shift observed between the heating and cooling data in the single-pulse method is very small, and can not even be safely ascribed to a genuine hysteresis as encountered in most of the FOTs. In fact, it appears that this hysteresis quantitatively corresponds to the expected temperature lag between the sample and the platform which contains the thermometer. At this stage, one must conclude that the transition at T_N is either a SOT or a very weakly FOT. Further information might be derived from the analysis of the critical behavior around T_N , but this will require measuring $C(T)$ for an isostructural non-magnetic compound to provide an accurate estimate of the lattice contribution more precise than a simple extrapolation of a Debye function. This work is currently in progress.

Below 43K, long-range magnetic order is detected by the presence of five additional Bragg peaks in the powder neutron diffraction data, the most intense close to a d-spacing of

4.5 Å. The intensity of these peaks decreases with the modulus of the scattering vector (Q) in agreement with the expected Q -dependence of the magnetic form factor. To determine the periodicity of the magnetic structure, an automatic indexing procedure using a grid search¹⁸ was employed but failed to give a satisfactory solution due to the presence of pseudo-trigonal symmetry. However, the magnetic peaks could all be indexed by exploring reciprocal space in the vicinity of the special k -vector expected for a 120° structure in a isotropic triangular lattice, corresponding to $\mathbf{k}=(0, \frac{1}{3}, 0)$ in the α -CaCr₂O₄ orthorhombic unit-cell. Further analysis shows that the magnetic structure is actually incommensurate with a propagation vector $\mathbf{k}=(0, 0.3317(2), 0)$, labelled k_8 in Kovalev's notation¹⁹. The incommensuration, albeit small, is genuine as indicated by the inferior refinement presented in Fig. 4 showing an offset for the position of the magnetic peak (most noticeable in the difference curve) when the value is locked at $\mathbf{k}=(0, \frac{1}{3}, 0)$. The profile of the magnetic peaks are almost purely Lorentzian and their widths are much larger than the instrumental resolution, indicating short correlations lengths. In order to account for the observed profile and derive an accurate value for the moment magnitudes, the Rietveld refinement of the magnetic phase was conducted using a phenomenological description of the peak broadening by a spherical harmonics expansion consistent with the Laue class mmm .

Irrep.	$\{2_x \frac{1}{2} 00\}$	$\{2_y 0\frac{1}{2}0\}$	$\{2_z \frac{1}{2}\frac{1}{2}0\}$	$\{\bar{1} 000\}$	$\{m_y \frac{1}{2} 00\}$	$\{m_{xz} 0\frac{1}{2} 0\}$	$\{m_{xy} \frac{1}{2}\frac{1}{2} 0\}$	$\{1 010\}$
Δ_1	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} \epsilon & 0 \\ 0 & \epsilon^* \end{pmatrix}$	$\begin{pmatrix} 0 & \epsilon^* \\ \epsilon & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & \epsilon^* \\ \epsilon & 0 \end{pmatrix}$	$\begin{pmatrix} \epsilon & 0 \\ 0 & \epsilon^* \end{pmatrix}$	$\begin{pmatrix} \epsilon^2 & 0 \\ 0 & \epsilon^{*2} \end{pmatrix}$
Δ_2	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \epsilon & 0 \\ 0 & \epsilon^* \end{pmatrix}$	$\begin{pmatrix} 0 & -\epsilon^* \\ -\epsilon & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & \epsilon^* \\ \epsilon & 0 \end{pmatrix}$	$\begin{pmatrix} -\epsilon & 0 \\ 0 & -\epsilon^* \end{pmatrix}$	$\begin{pmatrix} \epsilon^2 & 0 \\ 0 & \epsilon^{*2} \end{pmatrix}$

TABLE I. Matrix representatives of the complete irreducible corepresentations Δ_1 and Δ_2 associated with the irreducible representations of the little group τ_1 and τ_2 ¹⁹ (see text for details). The matrices act each on the two-dimensional spaces spans by the complex order parameters, respectively (η_1, η_1^*) and (η_2, η_2^*) . The matrix for time-reversal is not shown.

Symmetry analysis using the group of the propagation vector (little group) show that the magnetic representation for each Cr sites is decomposed in four irreducible representations, labelled τ_1 to τ_4 according to Kovalev's tables¹⁹. The magnetic structure is only compatible with a model that mix a basis vector along the $(1,0,0)$ direction that transforms as τ_1 , and a

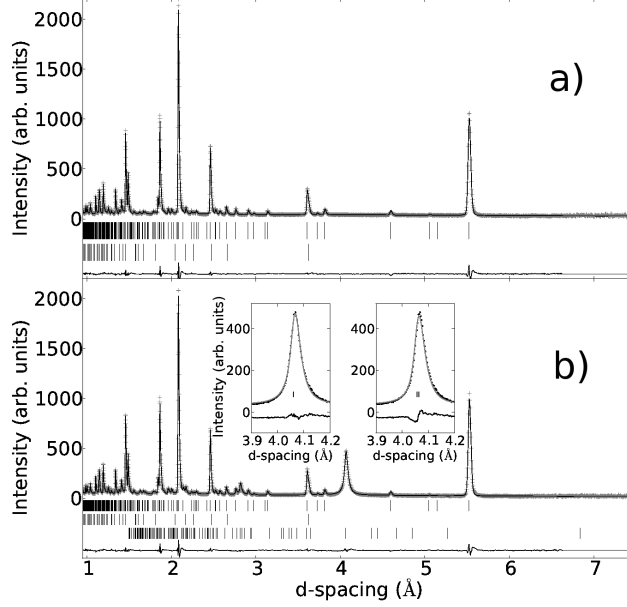


FIG. 4. Rietveld refinements of the neutron diffraction data collected in the paramagnetic phase at 70K (a) and in the magnetically ordered phase at 1.5K (b). The data are shown as grey points and the result of the refinements as continuous black lines. The curve shifted below represent the differences between observed and calculated patterns. In both panels, the top two rows of tick marks indicate the positions of Bragg peaks for the phases α - CaCr_2O_4 and the impurity Cr_2O_3 . In panel b, the third row of tick marks indicated the positions of magnetic Bragg peaks with propagation vector $\mathbf{k}=(0,0.33,0)$.

basis vector along $(0,0,1)$ that transform as τ_2 . In this orthorhombic symmetry, the intensity of the diffraction pattern is not sensitive to the relative phase between these two modes, i.e. one can not directly discriminate between a transversally polarized spin-density wave with the moments pointing in the ac -plane (mixing the two basis vectors with coefficients of same characters) or a helical modulation with the moment rotating in the ac -plane (mixing the two basis vectors with coefficients of different characters, real and imaginary). However at 1.5K, the refined amplitudes of the magnetic modes along the a and c axis were found to be $2.31(1) \mu_B$. If these modes were in phase (spin-density wave) the amplitude of the modulation will largely exceed the fully ordered moment of $3 \mu_B$ expected for a pure spin-state Cr^{3+} ion. On this ground, it appears that the helical modulation is the only possible model to account for the observed pattern. It is also physically sensible as the entropy of an helical structure with constant moments is more favorable at low temperature than an

amplitude modulated structure. The magnitudes of the magnetic moments were found to be similar for the two symmetry inequivalent Cr sites, and final refinements were conducted imposing such constraint, even if the latter is not directly imposed by symmetry. Finally, the relative phase between the modulation for site 1 and site 2 is a free parameter, as these sites are not related by symmetry operations of the group. The phase has been refined to a value very close to $-\frac{\pi}{3}$ and was constrained to this specific value in the final refinement. The magnetic structure, showed in Fig. 1, is made of nearly 120° configuration in each triangle, propagating as spirals along the b -axis of the unit-cell with the two spirals per unit-cell (on different Cr sites) of same chirality. Unlike cycloidal modulations, this proper spiral structure possess a true handedness. The coupling between adjacent CrO_2 layers, mediated through super-superexchange interactions, is antiferromagnetic. The magnetic structure is similar to that found in delafossites^{6,10}, i.e. the 120° configuration is *out-of-plane*. However, symmetry considerations lead to different coupling between magnetic order parameters and electric order than the delafossite, that will be discussed later. The ordered magnetic moment varies smoothly with temperature (Fig. 5) but the critical exponent was found to be $\sim \frac{1}{4}$, deviating largely from the mean-field limit and reminiscent to that found in first-order phase transitions²⁰. Within the temperature resolution of our experiment there is a unique transition at T_N , in agreement with measurements of the magnetic susceptibility and specific heat.

The magnetic model consists of a mixing of two modes belonging to two different irreducible representations, i.e. the transition from the paramagnetic phase to the incommensurate magnetic phase can be fully described by considering two two-dimensional complex order parameters $\eta_1 = \rho_1 e^{i\phi_1}, \eta_1^* = \rho_1 e^{-i\phi_1}$ and $\eta_2 = \rho_2 e^{i\phi_2}, \eta_2^* = \rho_2 e^{-i\phi_2}$. The matrix representatives of the complete irreducible co-representations of the group of \mathbf{k} are presented in Table I. The time-reversal operator $1'$, which matrix is not shown, needs also to be considered to be able to write the Landau energy. Considering these two magnetic order parameters, the expansion of the Landau free energy F is written:

$$F = F_0 + \frac{1}{2}\alpha_1\rho_1^2 + \frac{1}{2}\alpha_2\rho_2^2 + \frac{1}{4}\beta_1\rho_1^4 + \frac{1}{4}\beta_2\rho_2^4 \quad (1)$$

$$+ \gamma\rho_1^2\rho_2^2\cos(2\phi) + \dots \quad (2)$$

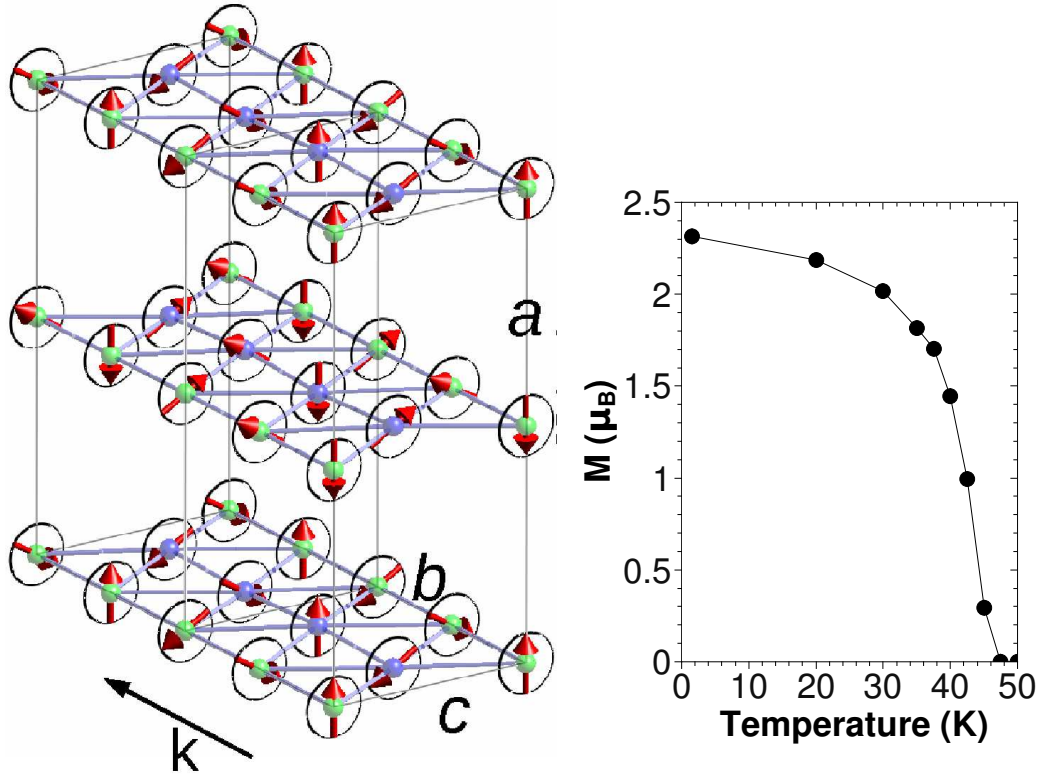


FIG. 5. (Color online) Left: Magnetic structure of α - CaCr_2O_4 . The two independent Cr sites are shown with different colors (light green for Cr_1 and light blue for Cr_2). Two unit-cells along the b -axis, marked by thin black lines, are shown. The axes are labelled in italic and the direction of the magnetic propagation vector (k) is shown by the arrow. Right: Temperature-dependence of the ordered magnetic moment on the Cr ions

, where the α_i , β_i ($i=1,2$) and γ are the usual coefficients and $\phi = \phi_1 - \phi_2$ is the phase difference between the two modes. Minimization of F with respect to ρ_1 and ρ_2 leads to five distinct magnetic states that can be stabilized from the paramagnetic space group $Pm\bar{m}n1'$. The point groups of these five magnetic states are shown in Fig. 6 together with their stability conditions. The structure observed experimentally corresponds to both order parameters being non-zero and $\phi = \pi/2$ (mixing of two modes in phase quadrature) and has the point symmetry $2221'$. The $1'$ operator is contained in the point group of any incommensurate structure, since its application (phase of π) is always equivalent to a translation. The phase $2221'$ can be stabilized from the paramagnetic state either through two successive second-order phase transitions as indicated by the arrow in Fig. 6 or through

a single first-order phase transition. According to our data showing a unique critical point but no pronounced hysteresis, we assumed that the transition must be *weakly* first-order. One should note that the only possibility to stabilize the observed magnetic phase through a second-order transition would be to consider a symmetry for the exchange Hamiltonian that is higher than the crystal symmetry (for example considering an Heisenberg Hamiltonian). In such case, the symmetry analysis shows that the two irreducible representations involved, τ_1 and τ_2 , belongs to the same exchange multiplet. However, this is rarely observed and always a case of pseudo-symmetry. In the following discussion, we will assume that the crystal symmetry is the relevant basis of work, and that the transition is weakly first-order.

The Landau theory of transitions with two order parameters that are coupled bi-quadratically has been studied by several authors^{21,22} and reviewed by Toledano et al.²³. The invariant as written in Eq. 2 is not sufficient to stabilize a first-order transition $\text{Pmmn1}' \rightarrow 2221'$ which would have to occur at a single point in the parameter space. In order to stabilize this transition through a line in phase space, one needs to consider a strongly negative coupling term γ and at least one positive six degree term (for example $\delta\rho_1^6$). In such conditions, considering that the first coefficient α_1 follows the usual temperature dependence $\alpha_1 = \alpha(T - T_c)$ with $\alpha > 0$, and that η_1 is the driving order parameter, the critical behavior of η_2 follows the triggering mechanism first discussed by Holakovsky²⁴.

The symmetry of this helical phase in such orthorhombic symmetry is extremely interesting. As already mentioned, the point group $2221'$, although not centrosymmetric, is not polar and therefore forbids a spontaneous polarization at the magnetic transition. Since the structure is incommensurate and the time-reversal operator is present in the point group, the linear magnetoelectric effect is also forbidden. However, invariants that are linear in the electric field (E) and quadratic in the magnetic field (H) are allowed by symmetry (whilst terms in HHE are forbidden). The quadratic magnetoelectric effect is described by a third-rank tensor, β_{ijk} symmetric in the last two indices and where i is the direction of the electric field and j and k indicate the direction of the magnetic fields. For the point group $2221'$ there are three terms allowed for this tensor that transform as the piezoelectric tensor, β_{123}, β_{213} and β_{312} . One can easily show using the matrix representatives of Δ_2 and Δ_3 given in Tab. I that the following mixed invariants of the magnetic order parameters with E and H can be constructed:

$$F_{ME} = \rho_1 \rho_2 \sin(\phi) [\beta_{123} E_x H_y H_z + \beta_{213} E_y H_x H_z + \beta_{312} E_z H_x H_y] \quad (3)$$

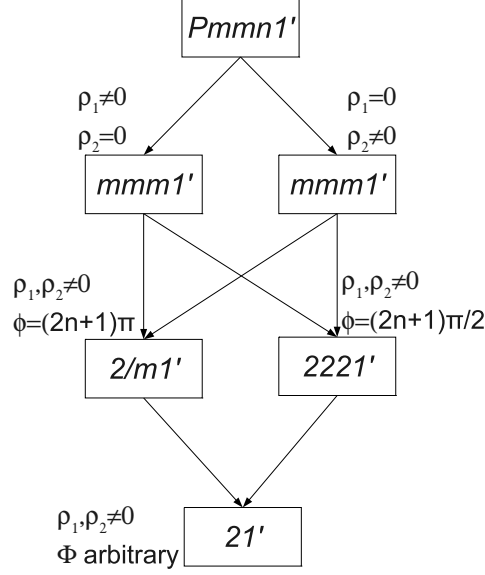


FIG. 6. Phase diagram of the possible magnetic point groups that can be stabilized from the paramagnetic group $Pmmn1'$ by considering two order parameters η_1 and η_2 transforming respectively as the τ_1 and τ_2 representations (see text for details).

This suggests that the application of low magnetic fields (if the system remains in the phase described by the symmetry of the zero-field phase) inclined with respect to the crystallographic axes will induce an electrical polarization whose magnitude will be proportional to the square of the magnetic field. Of course, the application of sufficiently large magnetic fields could drive the system to other symmetry phases. Single crystal specimens are necessary to determine the behavior of the electric properties and magnetic properties under a magnetic field.

It is important to realize that this result can be easily generalized to all incommensurate magnetic systems that possess a true magnetic handedness, i.e. all spirals in the unit-cell propagate with the same chirality. In such systems and irrespective of the paramagnetic symmetry, all improper symmetry operations are lost in the magnetically ordered state and the time-reversal operator is preserved by the incommensurability, implying that at least one of the β_{ijk} is allowed and quadratic magnetoelectric effects are present. This magnetoelectric effect, even though of higher degree in the expansion of the free energy than the well-studied linear effect, is not bounded by thermodynamic conditions (see²⁵ and references therein) and therefore interesting to investigate in prototype spiral magnets of the type discussed here.

In conclusion, measurements of the magnetic properties of α -CaCr₂O₄ and neutron powder diffraction have shown that this system is analog to the delafossite. Strong antiferromagnetic interactions in the triangular CrO₂ planes leads to long-range magnetic ordering below $T_N=43\text{K}$, with an incommensurate propagation vector $\mathbf{k}=(0,0.3317(2),0)$. The model for the magnetic structure, based on refinement of the neutron diffraction data and symmetry considerations, is consistent with an helicoidal modulation and a nearly 120° configuration in each triangular plaquette. The mirror plane symmetries are broken by the helicoidal arrangement, leaving the point group $2221'$, which allows for quadratic magneto-electric effects in all directions.

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- ¹ M. Kenzelmann, A. Harris, S. Jonas, C. Broholm, J. Schefer, S. Kim, C. Zhang, S. Cheong, O. Vajk, and J. Lynn, Phys. Rev. Lett. **95** (2005).
 - ² I. A. Sergienko and E. Dagotto, Phys. Rev. B **73**, 094434 (2006).
 - ³ H. Katsura, N. Nagaosa, and A. V. Balatsky, Phys. Rev. Lett. **95**, 057205 (2005).
 - ⁴ M. Mostovoy, Phys. Rev. Lett. **96**, 067601 (2006).
 - ⁵ M. Kenzelmann, G. Lawes, A. B. Harris, G. Gasparovic, C. Broholm, A. P. Ramirez, G. A. Jorge, M. Jaime, S. Park, Q. Huang, A. Y. Shapiro, and L. A. Demianets, Phys. Rev. Lett. **98**, 267205 (2007).
 - ⁶ K. Kimura, H. Nakamura, K. Ohgushi, and T. Kimura, Phys. Rev. B **78**, 140401 (2008).
 - ⁷ T. Kimura, J. C. Lashley, and A. P. Ramirez, Phys. Rev. B **73**, 220401 (2006).
 - ⁸ T. Nakajima, S. Mitsuda, S. Kanetsuki, K. Tanaka, K. Fujii, N. Terada, M. Soda, M. Matsuura, and K. Hirota, Phys. Rev. B **77**, 052401 (2008).
 - ⁹ T. Nakajima, S. Mitsuda, K. Takahashi, M. Yamano, K. Masuda, H. Yamazaki, K. Prokes, K. Kiefer, S. Gerischer, N. Terada, H. Kitazawa, M. Matsuda, K. Kakurai, H. Kimura, Y. Noda, M. Soda, M. Matsuura, and K. Hirota, Phys. Rev. B **79**, 214423 (2009).
 - ¹⁰ M. Poienar, F. Damay, C. Martin, V. Hardy, A. Maignan, and G. André, Phys. Rev. B **79**, 014412 (2009).
 - ¹¹ T. Arima, Journal of the Physical Society of Japan **76**, 073702 (2007).
 - ¹² H. Pausch and H. K. Müller-Buschbaum, Zeitschrift für anorganische und allgemeine Chemie **405**,

- 113 (1974).
- ¹³ PPMS Heat Capacity Option Users Manual, Quantum Design(2009).
 - ¹⁴ J. Hwang, K. Lin, and C. Tien, Rev. Sci. Instrum. **68**, 94 (1997).
 - ¹⁵ V. Hardy, Y. Brard, and C. Martin, J. Phys. Cond. Matter **21**, 075403 (2009).
 - ¹⁶ J. Lashley, M. Hundley, A. Migliori, J. Sarrao, P. Pagliuso, T. W. Darling, M. Jaime, J. Cooley, W. Hulst, L. Morales, D. Thoma, J. Smith, J. Boerio-Goates, F. Woodfield, G. Stewart, R. Fisher, and N. Phillips, Cryogenics **43**, 369 (2003).
 - ¹⁷ A. Szewczyk, M. Gutowska, B. Dabrowski, T. Plackowski, N. Danilova, and Y. Gaidukov, Phys. Rev. B **71**, 224432 (2005).
 - ¹⁸ J. Rodriguez-Carvajal, Physica B **192**, 55 (1993).
 - ¹⁹ O. Kovalev, *Representation of the Crystallographic Space Groups* (Gordon and Breach Science Publishers, 1993).
 - ²⁰ J. Toledano and P. Toledano, *The Landau theory of Phase Transitions* (World Scientific, 1987).
 - ²¹ J. Holakovsk, Physica Status Solidi (b) **56**, 615 (1973).
 - ²² Y. Ishibashi, Journal of the Physical Society of Japan **63**, 2082 (1994).
 - ²³ P. Toledano and V. Dmitriev, *Reconstructive Phase Transitions: In Crystals and Quasicrystals* (World Scientific Publishing, 1996).
 - ²⁴ J. Holakovsky, Phys. Stat. Sol. b **56**, 615 (1973).
 - ²⁵ W. Eerenstein, N. D. Mathur, and J. F. Scott, Nature **442**, 759 (2006).